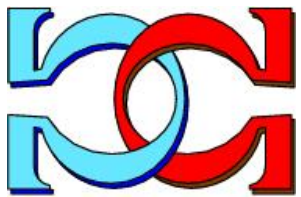
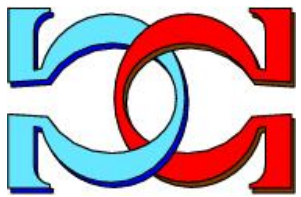
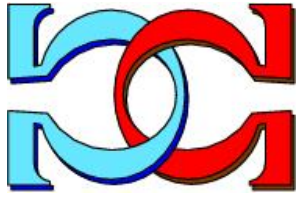
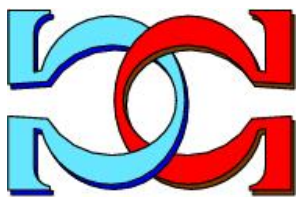


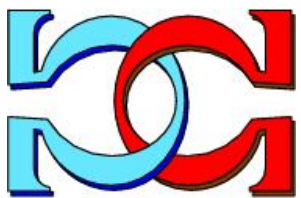
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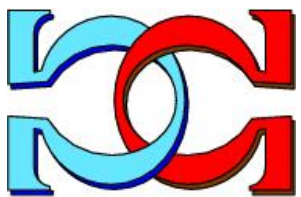
**Can a computer be “pushed”
to perform faster-than-light?**



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Can a computer be “pushed” to perform faster-than-light?

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Abstract. We propose to “boost” the speed of communication and computation by immersing the computing environment into a medium whose index of refraction is smaller than one, thereby trespassing the speed-of-light barrier.

The Church-Turing and the Cook-Karp theses, as well as other, more general limits on computation, are under permanent “scrutiny” (cf., e.g., Ref. [1, p 11] or Ref. [2, p. 5]) by the physical sciences. Some recent issues which have been raised comprise Zeno-squeezed accelerated time scales [3–7] enabling the construction of “infinity machines” capable of hypercomputation [8–10], counterfactual computation [11] and cryptography [12] based on quantum counterfactuals [13, 14], as well as the dissipation limits to computation [15]. Here we shall consider the possibility to speed up optical [16] computations and communication by transgressing the speed of light barrier in vacuum. Note that, although the speed of light barrier appears to be a fundamental limit for the transfer of “freely willable” information [17], several ways for “signals” trespassing the relativistic light cone [18], even to the extent of time travel [19–23], have been proposed. There appears to be a consensus that, just as for quantum correlations featuring (un)controllable non-locality [24] *via* outcome dependence but parameter dependence, “signal” signatures beyond the velocity of light limit [25] could be tolerated at the kinematical level [26] as long as they are “benign” and thus incapable of rendering diagonalization-type [1, 27] paradoxes.

In what follows we propose to “boost” the speed of communication and computation by “pushing” the computer into a medium whose index of refraction is smaller than one. The speed of communication by light signals varies indirectly proportional to the index of refraction, differing greatly for various forms of media, substrata or “ethers” susceptible of the traversal of light. Quantum field theory allows the index of refraction to become smaller than one, thereby formally indicating a speed of photons exceeding the classical speed of light limit in vacuum.

“Diagrammatically speaking” [28–30], i.e., in terms of perturbative quantum field theory, a photon, i.e., the “unit quantum of light” associated with a particular mode of the electromagnetic field, travels through the vacuum ether

medium [31] by polarizing it through partly “splitting up” into an electron-positron pair and recombining. In solid state physics, this phenomenon gives rise to lattice excitations called *phonons* [32]. The electrons and positrons are themselves subject to higher order radiative corrections involving photons.

Thus, any change of vacuum polarization, such as finite boundary conditions, or increased or decreased pair production, alters the susceptibility of the vacuum ether medium for carrying electromagnetic waves, and thus results in a change of the velocity of light. Historically, this effect has first been studied for magnetic fields [33–35] and finite temperatures [36]. The first indication of a vacuum polarization-induced index of refraction *smaller than one* was reported by Scharnhorst [37–39] and Barton [40, 41] in an attempt to utilize the reduced vacuum polarization in the “Casimir vacuum” [42] between two conducting parallel plates. More recently, trans-vacuum-speed metamaterials [43–47] as well as negative refractive indices in gyrotropically magnetoelectric media [48] have been suggested. It would be interesting to extend these calculations to the squeezed vacuum state by computing the polarization in such an “exotic” vacuum [49].

One of the possibilities which have not been discussed so far is the immersion of the computing environment into a vacuum ether medium “filled” with electrons or positrons. In such an environment, the Pauli exclusion principle would “attenuate” pair creation, thereby reducing the polarization of the medium, resulting in a reduced index of refraction as well as in an increase of the velocity of light.

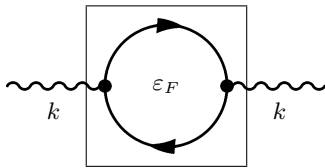


Fig. 1. Lowest order vacuum polarization diagram.

After regularization and renormalization, the lowest order change to the radiative correction associated with the vacuum polarization (whose Feynman diagram is depicted in Fig. 1) can be written as [50, 51, 29]

$$\Delta\Pi_{\mu\nu}(k^2) = - (g_{\mu\nu}k^2 - k_\mu k_\nu) \frac{2\alpha}{3\pi} \log \frac{\varepsilon_F}{m}, \quad (1)$$

where m stands for the electron rest mass and ε_F denotes the cutoff associated with the filled electron or positron modes; the calculation assumed $k^2 < m$. Let ϵ_μ stand for the vacuum polarization. Then we can introduce an effective mass term [52–54]

$$M(k) = \epsilon^\mu \Pi_{\mu\nu}(k) \epsilon^\nu \quad (2)$$

such that the eigenvalue equation is

$$\mathbf{k}^2 + M(k) = (k^0)^2, \quad (3)$$

where $k^\mu = (\mathbf{k}, k^0 = \omega)$; and

$$|\mathbf{k}| \approx \omega - \frac{1}{2\omega}M(k). \quad (4)$$

Thus the index of refraction can be defined by

$$n(\omega) = \frac{|\mathbf{k}|}{\omega} \approx 1 - \frac{1}{2\omega^2}M(k). \quad (5)$$

Hence the change of the refractive index is given by

$$\Delta n(\omega) \approx -\frac{\alpha}{3\pi\omega^2}(\epsilon^\mu k_\mu)^2 \log \frac{\epsilon_F}{m}. \quad (6)$$

As a result, the speed of light $c/(1 - \Delta n) \approx c + \Delta c$ is changed by $\Delta c = c\Delta n$.

As has already pointed out, this effect can be used to “push” the computer into a domain of faster-than-light communication; with the possibility to decrease its time cycles accordingly. One should keep in mind that at present such a possibility merely remains a theoretical speculation; this hypothetical character being shared with some relativistic “realizations” of hypercomputers. Nevertheless it might be interesting to pursue the possibilities related to temporal quantum field theoretical speedup further, for in principle nothing prevents Δn in Eq. (6) or in other “exotic” vacuum states from approaching one, yielding an unbounded cycle speed, associated with expanding memory requirements [55].

In summary we have discussed field theoretic options for the “speedup” of communication and computation. These are based on the alteration of the polarization of “exotic vacua” and the respective changes of the index of refraction. It should be emphasized that these findings do not represent the possibility to circumvent relativistic causality, nor are they inconsistent with the present formalism of relativity theory or the theory of quantized fields.

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