

RESEARCHSPACE@AUCKLAND

http://researchspace.auckland.ac.nz

ResearchSpace@Auckland

Copyright Statement

The digital copy of this thesis is protected by the Copyright Act 1994 (New Zealand).

This thesis may be consulted by you, provided you comply with the provisions of the Act and the following conditions of use:

- Any use you make of these documents or images must be for research or private study purposes only, and you may not make them available to any other person.
- Authors control the copyright of their thesis. You will recognise the author's right to be identified as the author of this thesis, and due acknowledgement will be made to the author where appropriate.
- You will obtain the author's permission before publishing any material from their thesis.

To request permissions please use the Feedback form on our webpage. http://researchspace.auckland.ac.nz/feedback

General copyright and disclaimer

In addition to the above conditions, authors give their consent for the digital copy of their work to be used subject to the conditions specified on the Library Thesis Consent Form.

THE EFFECT OF ALUMINA PROPERTIES AND SMELTER OPERATING CONDITIONS ON THE DISSOLUTION BEHAVIOUR OF ALUMINA

GERDA INGRID KUSCHEL

Thesis submitted for the degree of Doctor of Philosophy at the Department of Chemical and Materials Engineering, The University of Auckland, New Zealand.

Abstract

Alumina performs several functions in a modern smelter - it is used to scrub the pot gases to remove fluoride, acts as a thermal insulator on top of the cell and, when added to cryolite-based electrolytes, it is the raw material used to produce aluminium. Alumina is also expected to have good flow and handling properties, and dissolve well in the bath. Unfortunately, it does not always dissolve rapidly and this leads to the formation of "sludge", which creates operating disturbances in the cell; it is difficult to remedy this problem without a basic understanding of the process of alumina dissolution. Consequently, the objective of the work presented in this thesis was to develop an apparatus and technique that would allow the dissolution behaviour of powder alumina to be measured as realistically and objectively as possible, and then determine the important factors affecting dissolution.

The method developed involved the merging of three different techniques:

- electroanalytical measurement of dissolved oxide concentrations
- recording of the associated thermal phenomena
- visual observation of the interaction of alumina with the bath

which were then used to investigate the effect of a range of alumina properties and smelter operating conditions on dissolution behaviour. A series of dissolution parameters was selected to evaluate the relative dissolution behaviour of the different variables.

It was found that slow dissolution behaviour resulted primarily from poor feeding and/or dispersion, coupled with poor heat transfer in the first few seconds of the dissolution process.

If the flow properties of the alumina were good, alumina flowed easily out of the dropper on to the surface of the bath forming relatively thin but well-distributed rafts. If not, alumina could flow out into a localized area producing very dense rafts which clumped together and eventually sank to the bottom forming sludge. Properties such as loss on ignition enhanced the dispersion of the alumina through the release of volatiles, which caused the alumina to "effervesce" on the surface. Conversely, bulk density aggravated the clumping problem as the density of the formed rafts increased with increasing bulk density.

Good feeder design can help to counteract deficiencies in the flow properties of an alumina, if the importance of wide coverage and the imparting of a horizontal velocity component to the alumina are kept in mind. It was also found that if the bath agitation was increased, either by increasing the amount of existing stirring or by reducing the bath volume in the feeding area for a given bath velocity, the initial heat transfer to the alumina could be dramatically improved. The presence of bath superheat was important for maintaining optimum heat transfer conditions for fast dissolutions, as alumina was found to dissolve better when a higher proportion of the heat required was supplied from the bulk of the liquid bath as opposed to localized freezing.

Increasing the initial alumina concentration in the electrolyte retarded the dissolution process, with the retardation becoming increasingly more significant at higher concentration values. Similarly, reducing the cryolite ratio, which also decreased the alumina solubility, resulted in the dissolution being inhibited in the later stages, as more alumina dissolved. In situations where the mass transfer in the bath was improved, the impact of these concentration effects was minimized.

The video recordings were useful for indicating potential operating difficulties with the samples, such as excessive emissions and flow problems. Six different raft formations, characterizing the degree of bath surface coverage and the raft density or cohesion, were identified from the videos and the aluminas were classified accordingly.

Preliminary heat balance calculations were performed using the data obtained in this study and were used to estimate the heat of dissolution for α -Al₂O₃, for a variety of alumina concentrations in cryolite-based electrolytes. The results indicated heat values of 112 ±15 and 55 ±5 kJ mol⁻¹ for alumina concentrations in the bath of 0.43 and 2.83 wt% respectively. Further work is necessary to refine these calculations, however.

Reacted ore was found to dissolve more slowly than parent virgin alumina but it was difficult to ascertain which property caused the difference - whether bulk density, flowability, influence of HF, or presence of other impurities. As a result, it is recommended that a series of dissolution runs be performed on reacted samples of different compositions to establish which property associated with reacted ore causes the problem.

Acknowledgements

I am grateful to my supervisor, Professor Barry J. Welch for providing valuable guidance and inimitable inspiration throughout the course of this research project. The generous financial assistance of Alcoa of Australia Ltd is gratefully acknowledged. The alumina samples, physical property data, and photomicrographs were supplied by the Research and Development Department of Alcoa's Kwinana alumina refinery. Bath chemical analyses were performed at Alcoa's Point Henry smelter, which also supplied reacted ores for testing. Sincere thanks are extended to all personnel concerned at the refinery and smelter, especially Tony Bagshaw, Gerald Roach, Glenn Reid, and Nolan Broad. The support of Professor Mark Wainwright and the staff of the Chemical Engineering Department at the University of New South Wales in Sydney, while I was there to conduct the literature review, is warmly appreciated.

I would also like to thank the following people for their help during the course of this project: Eric Sinclair for his craftmanship in furnace design, building, and repair; Tom Gray, the late Grant Rule, Craig Aitcheson and Tim Snape for their workshop skills; Eddie van den Bergen for his ability to machine electrode components so well and the other workshop staff who kept my rig alive and running, sometimes at very short notice; Barry Tricklebank for sharing his years of wisdom and experience in high temperature experiments; David Stringer and Gary Prentice for assisting with computer problems, both large and small; Graeme Barber for providing the initial computer programs from which the data processing software was developed; Professors John Fenton, John Moore, Graeme Wright for the many helpful technical discussions.

I am very grateful for the support and friendship of my fellow graduate students, especially Ann Fitchett, Janette Wood, Pare Keiha, and Rick Smith, which has helped tremendously to keep me going. Special thanks to our ex-secretary Elizabeth Sharland for her sense of humour and fun. Thankyou to the many others who have helped me in various ways over the past four years.

Peter Jenkins and my mum kindly assisted with proof-reading of the thesis.

Special thanks to my husband, Nigel Hill (of Sydney, Australia), who put up with a long-distance wife who, even when she was in the same country, was usually working on her thesis.

Last, but not least, I would like to record my thanks to Professor lan Medland for encouraging me to take up engineering as a career in the first place.

Contents

Abstra	act				1
					iii
	wledgen	nents			ix
	Figures				xiii
	Tables				XV
list of	Symbols	5			^,
1	Introd	uctio	n		1
•	Referen				2
	Helelel	1062			
2	Backg	roun	d	******	4
	Scope				4
	2.1	The F	Production of Alumina via the Bayer Process		4
			Bauxite		4
		2.1.2	Digestion		5
		2.1.3	Clarification		6
		2.1.4	Precipitation		6
		2.1.5	Calcination		6
	2.2	The I	Production of Aluminium using the Hall-Héroult		10
			Process		
		2.2.1	Söderberg vs. pre-baked anodes		11
		2.2.2	The electrolyte composition		11
		2.2.3	Superheat		12
		2.2.4	Cell feeding and feeder design		12
		2.2.5	Bath velocity		13
		2.2.6	Reacted ore		14
	2.3	Requ	uirements of an Ideal Alumina	*******	14
	2.4	Previ	ious Alumina Dissolution Studies	******	15
	Refere	nces			15

•	3.0		When Disselution of Alumina in Cryolite-Based Melts		17
3		uring 1	the Dissolution of Alumina in Cryolite-Based Melts		17
	Scope		To design		17
	3.1		ous Alumina Dissolution Techniques	*******	5
			Weight loss methods		18
			Classical visual methods		19
		3.1.3	Electroanalytical techniques		21
		3.1.4	Chemical analysis of bath		25
		3.1.5	Microcalorimetry		25
			Combined approach		26
	3.2	Desig	n of the Electroanalytical-Thermal-Optical (ETO)		27
			Apparatus		
		3.2.1	Process conditions for testing alumina dissolution		28
			behaviour		
		3.2.2	Size and design of the melt-containing crucible		29
		3.2.3	Stirrer design		30
		3.2.4	Furnace arrangement		31
		3.2.5	Electrode design		32
		3.2.6	Alumina feeding system		34
		3.2.7	Investigation and design of video recording facilities		38
		3.2.8	Furnace control system		42
		3.2.9	Data acquisition system		42
		3.2.10	Apparatus summary		44
	3.3	Desc	ription of Electroanalytical-Thermal-Optical (ETO)		47
			Technique Developed		
		331	Electroanalytical measurements of dissolved alumina		47
		0.0.	concentration		
		3.3.2	Thermal analysis		51
			Optical recording		52
			Limitations		52
	3.4		vare Development		53
	. 0.7		*		53
					55
	31				56
					56
	Doford		Data conversion contrare		57
	Refere	3.4.2 3.4.3	Bath liquidus software Alumina dissolution run software Preliminary analysis software Data conversion software		55 56

4	Exper	imental Procedure	 61
	Scope		61
	4.1	Calibration of Electrode Voltammogramme Area Data	 61
		4.1.1 Temperature dependence	61
		4.1.2 Concentration dependence	63
	4.2	Determination of Bath Liquidus Temperatures	 65
		4.2.1 Experimental method for bath liquidus determination	65
	4.3	Alumina Dissolution Run Procedure	 67
		4.3.1 Preparation before an experiment	67
		4.3.2 Procedure prior to the first alumina addition	68
		4.3.3 Alumina addition procedure	69
		4.3.4 Procedure after the last addition	70
		4.3.5 After an experiment	70
	Refere	ences	71
5	Deve	lopment of Data Processing and Analysis Procedures	 72
	Scope		72
	5.1	Preliminary Data Processing to DOS Txt Format	 72
		5.1.1 Temperature vs. time data	73
		5.1.2 Quantity of electricity vs. time data	74
	5.2	Quantity of Electricity to Concentration Conversion	 75
	5.3	Combined Analysis Technique for the Concentration Data	 76
		5.3.1 Negative exponential fitting	77
		5.3.2 Fourier transform analysis	80
		5.3.3 Selective filtering	81
		5.3.4 Data recombination	82
		5.3.5 Normalizing	83
	5.4	Measurement of Dissolution Parameters	 84
6	Descrip	tion of Alumina Samples and Operating Conditions	 87
	Scop		87
	6.1	Alumina Samples	 87
		6.1.1 Descriptions of the samples supplied	87
		6.1.2 Comparison of the physical properties	93
		6.1.3 Standard experimental conditions for testing samples	95

vi

			vii
	6.2	Operating Conditions	97
		6.2.1 Descriptions of the conditions investigated	97
		6.2.2 Comparison of the operating parameters	99
	Refere	nces	100
7	Resu	Its Interpretation and Discussion	101
	Scope	•	101
	7.1	Dissolution Time vs. General Operating Parameters	101
		7.1.1 Effect of alumina concentration	101
		7.1.2 Importance of heat transfer	104
		7.1.3 Importance of mass transfer	104
	7.2	Dissolution Time vs. Specific Operating Conditions	108
		7.2.1 Effect of feeder design	109
		7.2.2 Effect of bath agitation	111
		7.2.3 Effect of superheat	112
		7.2.4 Effect of cryolite ratio	113
	7.3	Dissolution Time vs. Calcination-Dependent Alumina	115
		Properties	
		7.3.1 Effect of L.O.I. and M.O.I.	115
		7.3.2 Effect of B.E.T. surface area	117
		7.3.3 Effect of alpha-alumina content	118
	7.4	Dissolution Time vs. Particle Interaction-Related	120
		Alumina Properties	
		7.4.1 Effect of loose and packed bulk density	120
		7.4.2 Effect of flow funnel time	122
		7.4.3 Effect of PH, PM, and PS particle size cuts	124
	7.5	Dissolution Time vs. Miscellaneous Parameters	126
		7.5.1 Effect of reacted ore	126
		7.5.2 Effect of different refineries	127
		7.5.3 Effect of pressure calcination	128
	7.6	Summary of the Effects of the Different Variables on	130
		Dissolution	
	Refere	ences	132

			viii
8	Gene	ral Discussion	138
	Scope		138
	8.1	Characterization of Alumina Samples from Video	138
		Observations	
		8.1.1 Potential operating problems	138
		8.1.2 Different raft formations	142
	8.2	Internal Friction Factor Concept for Raft Formation	152
	8.3	Thermal Effects Associated with Alumina Dissolution	154
	10-10-	8.3.1 Heat required for the dissolution process	154
		8.3.2 Heat supplied for the dissolution process	155
		8.3.3 Typical heats of dissolution	161
	Refere	nces	163
9	Conc	lusions and Recommendations	164
	9.1	Conditions which Promote Poor Dissolution Behaviour	164
		9.1.1 Effect of alumina properties	164
		9.1.2 Effect of smelter operating conditions	167
		9.1.3 Summary	168
	9.2	Recommendations for Future Work	169
		9.2.1 Effect of dry scrubbing and reacted ores	169
		9.2.2 Combined alumina property correlations to predict	169
		dissolution behaviour	
		9.2.3 Dissolution correlations with alumina mobility coefficient	170
		9.2.4 Refinement of the heat of dissolution calculations	170
		9.2.5 Visual observation in industrial smelter cells	171
		9.2.6 The last word	171
App	endices		
1	Gloss	ary of Terms	172
11	Comp	lete List of References	175
Ш	•	gs of Computer Programs and Macros	179
IV		dsheet Summaries of Dissolution Parameters	201
V	Graph	s of All Dissolution Results	236

List of Figures

_			
	Figure	Text	Page
	2.1	Flow sheet of the Bayer process.	5
	2.2	Dehydration sequence of α -alumina trihydrates in air. (a = slow heating, b = fast heating, c = fine particles)	7
	2.3	Changes in selected properties during calcination of α -alumina trihydrate for a specific parent hydrate. (a = B.E.T. surface area, b = density, c = residual water or L.O.I.)	8
	2.4	Scanning electron micrographs of four aluminas produced under different calcination conditions illustrating the structural differences. (Bars on the bottom of each photo are 10 μ m long.)	9
	2.5	Schematic of a typical Hall-Héroult pre-baked smelting cell.	10
	3.1	The different graphite stirrer designs evaluated using the cold temperature system.	30
	3.2	Schematic of the electrode.	33
	3.3a	The temperature dependence measurements using a graphite electrode tip.	35
	3.3b	The temperature dependence measurements using a vitreous carbon electrode tip.	35
Q.	3.4	Exploded view of the alumina dropper showing from left to right - the middle section, the second choke, the end section, and the flow spreader.	36
	3.5	Schematic of the view port arrangement showing the fibre optics inside the two sleeves.	40
	3.6a	Photo of the furnace crucible without colour adjustment.	41
	3.6b	Photo of the furnace crucible with colour adjustment.	41
	3.7	Schematic of the data acquisition system, showing the systems for thermal analysis (to the left) and the electroanalytical measurements (to the right).	43
	3.8	Schematic of the cell used for dissolution studies.	45

3.9	Layout of the furnace lid showing the relative locations of all furnace components.	46
3.10a	The repeatability of the voltammogrammes measured using the ETO apparatus at a constant initial alumina concentration. <u>Note</u> : each successive curve is displaced on the time axis.	49
3.10b	The repeatability of the voltammogrammes measured using the ETO apparatus at a constant initial alumina concentration. <u>Note</u> : the four curves are superimposed on the time axis.	49
3.11	The effect of increasing alumina concentration (in wt%) on the shape of the voltammogrammes.	50
3.12	A typical concentration-time profile for the dissolution of alumina powder.	50
3.13	A typical temperature-time profile for the dissolution of alumina powder illustrating the three stages (same sample as that used in Figure 3.12).	51
4.1	The temperature dependence of the quantity of electricity results using a graphite electrode.	62
4.2	A typical graph of the relationship between concentration and the temperature-corrected quantity of electricity values for an electrode.	63
4.3a	A typical cooling curve recorded for the standard bath composition indicating the liquidus occurring at 983.6 °C.	66
4.3b	A typical cooling curve recorded for the low ratio bath composition.	66
5.1	A comparison of the original concentration data with the negative exponential fit generated in "GFITHAN" (for KBFA_C1). Note: there is a flat initiation period occurring after the addition point (t=90s).	78
5.2	Diagram illustrating the high frequency components inherent in the raw concentration data (for KBFA_C1).	80
5.3	The amplitude <i>versus</i> frequency spectrum of the raw concentration data from Figure 5.2 (for KBFA_C1). The middle region is the noise floor and the outer regions represent the true data.	81
5.4	The amplitude spectrum of the Hann window filter file, GKH_08.FIL, compared to the spectrum of the actual data in Figure 5.3 (shown shaded in the background).	82
5.5	A comparison of the Fourier-smoothed results with the original concentration data and the negative exponential fit (for KBFA_C1).	83

5.6	Key indicators for the dissolution of alumina.	85
5.7	Other dissolution indicators.	86
6.1	Photomicrograph of the special hydrate, with a blockiness index of 1, used to produce SH7. (magnification is 250x)	89
6.2	Photomicrograph of the special hydrate, with a blockiness index of 8, used to produce SH5. (magnification is 250x)	90
6.3	Photomicrograph of the PCF3 alumina produced under typical calcination conditions in the laboratory calciner. (magnification is 250x)	90
6.4	Photomicrograph of the PCD alumina, typical Pinjarra calciner discharge. (magnification is 250x)	91
6.5	Photomicrograph of the PBF alumina, typical Pinjarra bin feed, to illustrate the effect of adding ESP dust. (magnification is 250x)	91
7.1a	t'50 and t'80 dissolution times versus increasing alumina concentration.	103
7.1b	t'66 and t'f dissolution times versus increasing alumina concentration.	103
7.2a	t'50 and t'80 dissolution times <i>versus</i> increasing maximum temperature drop recorded by the bath, Tmax.	105
7.2b	t'66 and t'f dissolution times versus increasing maximum temperature drop recorded by the bath, Tmax.	105
7.3	The effect of decreasing the mass transfer (by increasing the bath mass) on the dissolution behaviour of 14 g of standard alumina with 200 rpm stirrer speed.	106
7.4	The effect of decreasing the mass transfer (by reducing the bath agitation) on the dissolution behaviour of 4.24 g of standard alumina in 600 g bath.	107
7.5	The four dissolution time indicators <i>versus</i> increasing loss on ignition.	116
7.6	The four dissolution time indicators <i>versus</i> increasing values of B.E.T. surface area.	117
7.7a	The effect of loose bulk density on the dissolution times in a well-agitated system.	121

7.7b	Dissolution trends for increasing loose bulk density in a poorly- agitated system.	121
7.8	The effect of increasing flow funnel time on the alumina dissolution process.	123
7.9	The effect of increasing the particle size of the PS fraction on the alumina dissolution process.	125
8.1	Photo sequence for "thin wispy/wide coverage" raft behaviour with alumina added at 1:30 on the timer (sample PCF6).	144
8.2	Photo sequence for "3 rafts/well-distributed" raft behaviour with alumina added at 1:30 on the timer (sample SH5).	145
8.3	Photo sequence for "clumping" raft behaviour with alumina added at 1:40 on the timer (sample PCF2).	146
8.4	Photo sequence for "small rafts/well-distributed" raft behaviour with alumina added at 1:40 on the timer (sample KSC).	148
8.5	Photo sequence for "steady flowing/moved to stirrer" raft behaviour with alumina added at 1:40 on the timer (sample PCD).	149
8.6	Photo sequence for "very dense rafts" raft behaviour with alumina added at 1:40 on the timer (sample PHRO).	150
8.7	Schematic of a cross-section through the carbon crucible used to contain the bath.	157
8.8a	A typical thermal analysis of the dissolution process, comparing the progress recorded for the alumina concentration data with that of the heat supplied (based on an average of both heat methods).	160
8.8b	The same thermal analysis as above highlighting the special features of the heat curve.	160
9.1a	The concentration-time profiles for a fast and a slower dissolving alumina (using a linear time scale).	165
9.1b	The same concentration-time profiles as in Figure 9.1a but for a reduced range (using a logarithmic time scale).	165
9.2a.	The corresponding temperature-time profiles for a fast and a slower dissolving alumina (using a linear time scale).	166
9.2b	The same temperature-time profiles as in Figure 9.2a but for a reduced range (using a logarithmic time scale).	166

List of Tables

Table	Text	Page
3.1	Summary of the processes that contributed to the overall dissolution time measurement for previous experiments using the MLSV technique.	28
3.2	Summary of the experimental software developed and the corresponding functions.	54
6.1a	Summary of the physical properties dependent upon calcination conditions for the alumina samples used in the dissolution study.	93
6.1b	Summary of the physical properties relating to particle interactions for the alumina samples used in the dissolution investigation.	94
6.2	Summary of the smelter operating conditions investigated for a standard alumina sample in the dissolution study.	99
7.1	Comparison of the average dissolution parameters measured for a standard alumina under the different smelter operating conditions investigated in the dissolution study.	108
7.2	Comparison of the average dissolution results for a normal 360° surface spreading feeder with those for a single point feeder (spf) design.	110
7.3	The effect of stirrer speed on the average dissolution parameters.	111
7.4	The effect of bath superheat on the average dissolution parameters.	113
7.5	The effect of reduced cryolite ratio on the average dissolution parameters.	114
7.6	The average dissolution parameters measured for reacted ore compared with those measured for potential parent virgin aluminas (both bin feed and calciner discharge).	127
7.7	A comparison of the average dissolution parameters for aluminas produced by calcining hydrate from the different refineries under standard calcination conditions (using both laboratory and industrial calciners).	127

7.8	A comparison of the average dissolution parameters for aluminas produced by pressure, laboratory, and industrial calcination.	129
7.9	Summary of the changes in alumina dissolution times for different smelter operating conditions.	130
7.10	Summary of the changes in alumina dissolution times for different alumina properties under standard operating conditions.	131
	4	
8.1	Summary of the alumina samples that exhibited potential operating difficulties.	139
8.2	Comparison of the physical properties relating to particle interaction for the alumina samples which experienced flow difficulties.	140
8.3	Comparison of the physical properties dependent upon calcination conditions for the alumina samples which caused excessive emissions.	141
8.4	Characterization of the rafts formed by different alumina samples.	143
8.5	Comparison of some of the physical properties for aluminas which did and did not exhibit "clumping" raft behaviour.	147
8.6	Comparison of some of the physical properties for reacted and virgin aluminas.	151
8.7	Typical heats of dissolution for α -Al $_2$ O $_3$ calculated using both methods for various alumina concentrations (in the bath) and different alumina samples.	161
8.8	Comparison of the heats of dissolution measured for $\alpha\text{-Al}_2\text{O}_3$ in cryolite-based melts by various workers.	162
9.1	Comparison of the ETO dissolution results that typically characterize good and poor alumina dissolution.	167
9.2	Summary of the conditions which can result in poor alumina dissolution behaviour.	168

List of Symbols and Abbreviations

Symbol	Description	Unit
A A ALPHA	a constant interfacial area between the crucible and the bath $_{\alpha}\text{-Al}_{2}\text{O}_{3}$ content	m ² wt%
b B BET SA	Tafel slope a constant B.E.T. surface area	V m ² g ⁻¹
C C	actual concentration at time t alumina concentration	kg m ⁻³ wt%
C C(1) C _{exp} C _p C _{pa} C _{pb,1260} C _{pc} C _{pc,1260} C _s C ₀ %C AC A%C _{F-s} A%C _{raw} Conc	a constant alumina concentration at the addition point negative exponential fit at time t heat capacity heat capacity of the solid alumina heat capacity of the bath heat capacity of the bath at 1260 K, 1.7970 J g ⁻¹ K ⁻¹ heat capacity of the graphite crucible heat capacity of the graphite crucible at 1260 K, 1.9173 J g ⁻¹ K ⁻¹ saturation concentration saturation concentration percent alumina concentration change, 0-100 % theoretical concentration change for the addition scaled Fourier-smoothed percent concentration change scaled raw percent concentration change alumina concentration cryolite ratio (wt NaF to wt AIF ₃)	cm ⁻³ or kg m ⁻³ % wt% % wt%
D D	diffusion coefficient a constant	m ² s ⁻¹
ESP	electrostatic precipitator	
f ₁ (x) f ₂ (x) F F F _g FFT	mathematical function of x, where x is a variable mathematical function of x, where x is a variable Faraday's constant, 9.652•10 ⁴ C mol ⁻¹ frequency of readings or seconds between readings mass fraction of the alumina that is non-alpha alumina, 0-1 flow funnel time per 100 g alumina sample	C mol ⁻¹ s min

h _x H H _{required}	heat transfer coefficient between the crucible and the bath Hann multiplication factor, 0-1 total heat required for the dissolution of alumina	W m ⁻¹ K ⁻¹ J
H _{supplied} H ₁	total heat supplied for the dissolution of alumina total heat supplied using the purely conductive heat transfer approach	kJ mol ⁻¹
H ₂	total heat supplied using the combined convective/conductive heat transfer approach	kJ mol ⁻¹
ΔH_{phase} ΔH_{diss}	heat for the phase transformation to α -Al $_2$ O $_3$ at 1260 K heat of dissolution	J mol ⁻¹ or J
i i	current density number of a point or reading	A cm ⁻²
i _p	peak current density	A cm ⁻²
k k _T k'	a constant temperature dependence constant at T °C a constant	
K K	dissolution rate constant total number of cycles	m s ⁻¹
K _{add}	number of the addition cycle	g I ⁻¹
LBD LOI LSV	loose bulk density loss on ignition (300-1000 °C) linear sweep voltammetry	wt%
m m _a	amount of alumina dissolved per unit time mass of alumina dissolving	kg m ⁻³ s ⁻¹ g
m _b m _c	mass of the bath mass of the crucible over which ΔT_c acts	g g
MLSV MOI	modified linear sweep voltammetry moisture on ignition (0-300 °C)	wt%
n	number of electrons tranferred	1
PBD PH	packed bulk density 90th percentile of the particle size distribution	g Γ ⁻¹ μm
PM PS	50th percentile of the particle size distribution 10th percentile of the particle size distribution	μm μm
q q _s	dynamic heat flux steady state heat flux or convective heat transfer rate	W or J s ⁻¹ W or J s ⁻¹
q _{xs} Q	increased heat flux area under the voltammogramme or quantity of electricity value	W or J s ⁻¹ C
r ·	radius of the sample disc average regression coefficient	m
r _{av} R	gas constant, 8.317 J mol ⁻¹ K ⁻¹	J mol ⁻¹ K ¹
spf S	single point feeder dissolution surface area	m^2

		xvii
t to Δt tinit t'50 t'66 t'80 t'f T T T T D T D T D T D T D T D T D T D	time at the end of the initiation period change in time initiation time time taken to reach 50 % dissolved minus tinit time taken to reach 66 % dissolved minus tinit time taken to reach 80 % dissolved minus tinit time taken to reach 100 % dissolved minus tinit time taken to reach 100 % dissolved minus tinit (based on initial rate of dissolution) temperature average temperature of the crucible wall bath temperature bath temperature crucible wall temperature bath operating temperature bath operating temperature for the 1st addition bath operating temperature for the 4th addition wall temperature of the outside of the crucible transient change in the bath temperature transient change in the crucible wall temperature bath temperature change or drop bath temperature change crucible wall temperature change or drop temperature-corrected quantity of electricity value (coulombs) maximum temperature drop recorded by the bath thermocouple	ος ο
v V	sweep rate solution volume	V s ⁻¹ m ³
w	width of the Hann window	
x	addition number, 1-4	
α α -Al ₂ O ₃ β -Al ₂ O ₃ γ -Al ₂ O ₃ δ -Al ₂ O ₃	angle of repose alpha alumina beta alumina gamma alumina delta alumina	٥
θ-Al ₂ O ₃ ν	theta alumina kinematic viscosity	m ⁻² s
π τ	a constant, ~ 3.141592654 transition time	S
φ χ-Al ₂ O ₃	angle of internal friction chi alumina	s ⁻¹
ω	angular velocity	S

To the memory of Fritz,

The best dog an engineer could have.