A technique for approximating the location of surface- and leaky-wave poles for a lossy dielectric slab

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A Technique for Approximating the Location of Surface- and Leaky-Wave Poles for a Lossy Dielectric Slab

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Abstract—An approximation technique for locating the surface- and leaky-wave poles for a lossy dielectric slab is presented. The problem is reduced to the simultaneous solution of two transcendental equations (for each of the perfect magnetic conductor (PMC) and perfect electric conductor (PEC) cases) which is shown to yield a simple approximate solution for the poles, and which can subsequently be refined using numerical optimization. The technique yields both surface-wave and leaky-wave poles, and results are presented for a typical example to demonstrate the approach. The greatest approximation accuracy was observed for surface-wave and leaky-wave poles well removed from the spectral gap. For poles either within or in close proximity to the spectral gap, an alternative iterative technique is proposed. Expressions for the number of proper plus improper surface-wave poles in a given problem are also derived.

Index Terms—Dielectric waveguides, electromagnetic surface waves, leaky waves.

I. INTRODUCTION

The lossy concrete slab with an embedded wire structure is of interest to radio system planners deploying broadband wireless communications services in indoor environments. Steel-reinforced concrete is a common building material, and is known to have a significant effect on the transmission of radio signals [1]. Recently, some attention has been focussed on the development of a Green’s function/method of moments (GF/MoM) solution for an infinite lossy dielectric slab with a two-dimensional embedded wire matrix [2], [3]. The near field solution to this problem reported in [2], [4] has shown that the presence of an internal wire structure significantly alters the behavior of the transmitted field.

A key requirement in the calculation of the Green’s functions for the slab geometry is the location of any relevant surface- and/or leaky-wave poles which are needed when evaluating the contour integral formulation. Techniques for locating the surface- and leaky-wave poles have been considered by a number of authors, e.g., [5, pp. 732–734]–[7]. However, these approaches usually consider the surface- and/or leaky-wave poles separately, or consider only the lossless case. In this paper, we present a technique for rapidly approximating both the surface- and leaky-wave pole locations for the lossy isotropic dielectric slab.

In Section II, the pole equations for the problem considered are presented. Techniques for approximating the surface- and leaky-wave poles for the perfect magnetic conducting (PMC) and perfect electric conducting (PEC) cases are presented in Sections III and IV, respectively. The relationship between the approximation technique and the well-known spectral gap are explored in Section V. The notion of a “split zone” introduced therein is used in Section VI to propose an improvement to the technique for poles which are either deeply within the split zone or for when large-conductivity substrates are being considered. Finally, expressions for the number of proper plus improper surface-wave poles in a given problem are derived in Section VII.

II. THE LOSSY DIELECTRIC SLAB

The same terminology used in [2] is employed in this paper. Specifically, a lossy dielectric slab (Region 2) with permittivity $\varepsilon_2$ and permeability $\mu_2$ is considered. The surrounding medium (Region 1) is characterized by $\varepsilon_1$ and $\mu_1$. An electric line source of strength $I_0$ is located in Region 1. The wavenumbers $k_1$ and $k_2$ for Region 1 and 2, respectively, are defined as $k_1 = \omega \sqrt{\mu_1 \varepsilon_1}$ and $k_2 = k_1 \sqrt{\mu_2 \varepsilon_2}$ where $\mu = (\mu_2/\mu_1)$ and $\varepsilon = (\varepsilon_2/\varepsilon_1)$. We are interested in characterizing the TM$_2$ field in this geometry, and the reader is referred to [2] for further details. Of relevance in this paper is the behavior of the PMC and PEC reflection coefficients, namely

$$\Gamma_m(\eta) = \frac{j \mu_1 \tan \kappa_2 d + \kappa_2}{j \mu_1 \tan \kappa_2 d - \kappa_2}$$

(1)

and

$$\Gamma_e(\eta) = \frac{j \mu_1 \cot \kappa_2 d + \kappa_2}{j \mu_1 \cot \kappa_2 d - \kappa_2}.$$  

(2)

The parameters $\kappa_1$ and $\kappa_2$ are given by

$$\kappa_1 = \sqrt{k_2^2 - \eta^2}$$

(3)

and

$$\kappa_2 = \sqrt{k_2^2 - \eta^2}.$$  

(4)

The solution for $\Gamma_m$ assumes a slab on a PMC ground, whereas $\Gamma_e$ assumes a slab on a PEC ground. In both cases the slab thickness is $d$. The presence of $\Gamma_m$ and $\Gamma_e$ in the integrand of the Green’s function ([(2, eq. (4))]) requires the determination of the poles of (1) and (2) prior to performing the contour integration.
Expression (3) introduces branch points at \( \eta = \pm k_1 \) and accordingly the Riemann surface for \( \Gamma(\eta) \) has two sheets. To remove these branch points it is convenient to make the substitution [8, pp. 462–464]

\[
\eta = k_1 \sin w.
\]

The regions where \( \text{Re}(w) > 0, \text{Im}(w) < 0 \) and \( \text{Re}(w) < 0, \text{Im}(w) > 0 \) correspond to values of \( \eta \) on the improper Riemann surface. The poles exhibit an odd symmetry with respect to the origin, but the presence of dielectric loss destroys the pole symmetries about the trajectories \( \text{Re}(w) = \pm \pi/2 \). The various poles are categorized as either surface wave (these can be either proper or improper depending on which Riemann sheet they fall) or leaky-wave (which are always improper). Equations (1) (PMC) and (2) (PEC) will each yield a set of poles for any given value of \( d \). It will thus be useful to explore solutions for each of these cases separately.

III. POLE SOLUTIONS—PMC CASE

We need to determine the values of \( \eta \) for which the denominator of (1) is zero, i.e.,

\[
j \mu k_1 \cos k_2 d - k_2 = 0, \quad (6)
\]

It can be shown that, if \( p = k_2 d \) and \( q = k_1 d \) then

\[
p^2 - q^2 = (\mu - 1)(k_1 d)^2 = \ell^2
\]

and

\[
ptan p = j\mu q.
\]

Assuming \( \mu = 1 \), and after some rearrangement of (7) and (8) it can be shown that

\[
p^2 + \tan^2 p = (\mu - 1)(k_1 d)^2 = \ell^2
\]

\[
\Rightarrow p \sec p = \pm \ell.
\]

If \( p = x + jy \), (9) can be separated into real and imaginary parts, and assuming a lossy material (so that \( \ell \) and therefore \( \ell \)) will be complex then

\[
\pm \ell = \pm (\ell_r + j\ell_i) = \frac{x + jy}{\cosh x \cosh y - j \sin x \sinh y}
\]

and so

\[
\pm [\ell_r \cosh x \cosh y + \ell_i \sin x \sinh y] - x = 0 \quad (10)
\]

and

\[
\pm [\ell_i \cos x \sinh y - \ell_r \sin x \cosh y] - y = 0 \quad (11)
\]

Simultaneous solution of (10) and (11) will yield \( x \) and \( y \) from which \( p \) and then \( \eta \) can be determined.

It is useful at this time to plot (10) and (11) in order to visualise the behavior of the desired solution. Unfortunately, these expressions are transcendental in form and are also multivalued. However, a simple way to plot functions of this type is to use a contour plotting package to plot a single contour at height 0. It should be noted from (9) that \( p \sec p \) is odd (both real and imaginary parts), and accordingly solutions for \( p \) will differ only in sign. As (1) and (2) are not dependent on the sign of \( p \), it is sufficient to only consider the positive solution, namely \( p \sec p = \pm \ell \).

As an example, consider a concrete slab \( (\epsilon_r = 6, \sigma = 1.95 \text{ mS/m}) \) which has a thickness \( d = 0.1 \text{ m} \) and an excitation frequency of 1.8 GHz [2]. Corresponding plots of (10) and (11) are given in Fig. 1. The result in Fig. 1 shows solutions of two different types, namely (a) a finite number of solutions (labeled 1 . . . 5) for (10) where \( y \approx 0 \); and (b) complex solutions (labeled A . . . H) for (10) separated by multiples of \( 2\pi \), namely \( x \approx (\pi, 6\pi, 8\pi, \ldots) \) for \( x > 0 \) and \( x \approx (\pm 3\pi, \pm 5\pi, \pm 7\pi, \ldots) \) for \( x < 0 \). This is a very useful observation, since these approximations for \( x \) are integer multiples of \( \pi \) and are not dependent on the physical geometry, material properties or frequency. Furthermore, this result suggests that solutions (a) correspond to the surface wave poles and (b) to leaky-wave poles. To test this hypothesis it will be useful to consider separate solutions in each of these regimes.

A. PMC Case—Surface-Wave Poles

Fig. 1 suggests that \( y \approx 0 \) for the surface-wave poles. The approximate location for the surface-wave poles can be found by substituting \( y = 0 \) in (10). Accordingly

\[
x = \pm \ell_r \cos x
\]

\[
\Rightarrow \ell_r \cos x = x = 0
\]

(12)

where the \( \pm \) has been dropped for the reason outlined previously. Estimates for \( x \) can be determined using a simple root finding algorithm. Given the predictable oscillatory nature of (12), a bracketing approach (such as bisection) is well suited to this role. Once these estimates have been obtained, using (4) it can be shown that

\[
\eta = \pm \sqrt{k_2^2 - \left(\frac{x}{d}\right)^2}.
\]

The question now arises as to which of the two possible Riemann sheets correspond to the solutions for \( \eta \) which produce poles. To determine the correct nature of these poles it is necessary to calculate \( \Gamma_m(\eta) \) using (1) for both the proper \( \text{Im}(k_1) < 0 \) and improper \( \text{Im}(k_1) > 0 \) Riemann sheets. This procedure will only yield a “large” value for \( \Gamma_m \) on either the proper or improper Riemann sheets, but not both.
Given this behavior, it is for approximations for and is located on and the approximation error should be replaced by

\( w = \sin^{-1}\left( \frac{\eta}{k_1} \right). \)

If the pole has \( \text{Im}(k_3) < 0 \) and is located on the improper Riemann sheet, or the pole has \( \text{Im}(k_3) > 0 \) and is located on the proper Riemann sheet, then \( w \) should be replaced by

\[ w = -w + \pi \]

thereby forcing the pole to lie in the correct location in the \( w \)-plane.

It must be noted that the values for \( w \) thus calculated are only approximations to the solution of \( (10) \) and \( (11) \). A much closer estimate of the pole locations can be obtained if multidimensional optimization is adopted using the approximate values calculated above as seeds. Estimates of \( x, y \), approximations for \( w \), an optimized estimate \( w' \) and the approximation error \( |w - w'| \) for the example being considered are listed in Table I. These approximate and optimized estimates for \( w \) are also shown in Fig. 2. The location of the poles labeled \( (1 \ldots 5) \) confirms the hypothesis that these poles are indeed surface-wave poles.

### B. PMC Case—Leaky-Wave Poles

A similar approach can be taken for the leaky-wave poles, by noting from Fig. 1 that complex solutions for \( (10) \) exhibit the same geometrical/material/frequency independent properties as the surface-wave poles in Section III-A. For the leaky-wave poles, the complex solutions are separated by approximately \( 2\pi \) and are located at \( x \simeq (4\pi, 6\pi, 8\pi, \ldots) \) for \( x > 0 \), and \( x \simeq (-3\pi, -5\pi, -7\pi, \ldots) \) for \( x < 0 \). Given this behavior, it is possible to rewrite \( (10) \) as

\[ y = \cos^{-1}\left( \frac{|\eta|}{k_1} \right). \]

The corresponding values of \( \eta \) and \( w \) can now be calculated, given that these poles must all by definition be located on the improper Riemann sheet. As with the surface-wave poles, the

1According to the definition \( \arcsin z = (-1)^k \arcsin z + k\pi \) where \( k \) is an arbitrary integer [9, p. 80].

## Table I

| Pole | \( x \) | \( y \) | \( w \) | \( w' \) | \( |w - w'| \) |
|------|-------|-------|-------|-------|----------|
| 1    | -4.19 | 0.0   | 1.57 + j1.42 | 1.57 + j1.41 | 6.82 \times 10^{-5} |
| 2    | -1.78 | 0.0   | 1.57 - j1.52 | 1.57 - j1.52 | 1.14 \times 10^{-5} |
| 3    | 1.40  | 0.0   | 1.57 + j1.53 | 1.57 + j1.53 | 5.42 \times 10^{-6} |
| 4    | 5.40  | 0.0   | 1.57 - j1.31 | 1.57 - j1.31 | 2.15 \times 10^{-4} |
| 5    | 6.90  | 0.0   | 1.58 + j1.07 | 1.57 + j1.07 | 5.29 \times 10^{-4} |
| A    | -9.42 | 0.48  | 2.75 - j0.67 | 2.70 - j0.61 | 8.11 \times 10^{-2} |
| B    | -9.42 | -0.48 | 0.40 - j0.68 | 0.46 - j0.62 | 8.47 \times 10^{-2} |
| C    | 12.57 | 0.95  | 0.15 - j1.57 | 0.15 - j1.55 | 1.64 \times 10^{-2} |
| D    | 12.57 | -0.95 | 3.00 - j1.57 | 2.99 - j1.55 | 1.56 \times 10^{-2} |
| E    | -15.17| 1.23  | 3.03 - j1.94 | 3.03 - j1.93 | 8.42 \times 10^{-3} |
| F    | -15.17| -1.23 | 0.11 - j1.94 | 0.12 - j1.93 | 8.84 \times 10^{-3} |
| G    | 18.85 | 1.44  | 0.098 - j2.18 | 0.099 - j2.18 | 5.95 \times 10^{-3} |
| H    | 18.85 | -1.44 | 3.04 - j2.18 | 3.04 - j2.18 | 6.66 \times 10^{-3} |

Once the correct sheet has been identified, an estimate for \( w \) can be made. Given the mapping operation \((5)\), we can calculate \( w \) from

\[ w = \sin^{-1}\left( \frac{\eta}{k_1} \right). \]

![Fig. 2. Plot of the \( w \)-plane for example showing locations of three proper surface-wave poles (1, 3, 5), two improper surface-wave poles (2, 4) and the first eight leaky-wave poles (A \ldots H) for the PMC case. (The initial approximations to the poles are shown by the "+" symbols, and the optimized estimates by the "o" symbols).](image-url)
IV. POLE SOLUTIONS—PEC CASE

In a manner similar to that in the PMC case, we need to determine the values of \( \eta \) for which the denominator of (2) is zero, i.e.

\[
j \mu k_1 \tan k_2 d + k_2 = 0.
\]

Given the same definitions for \( p \) and \( q \) as in Section III and the PEC “dual” of (8) namely

\[
-p \cot p = j \mu q
\]

rearrangement of (7) and (13) with \( \mu = 1 \) yields

\[
p^2 + p^2 \cot^2 p = (\epsilon - 1)(k_2 d)^2 = \ell^2 \\
\Rightarrow p \cot p = \pm \ell.
\]

(14)

It should be noted that the lossless case has already been considered by Collin [5, pp 732–734]. However, here we are interested in the lossy case, so defining \( p = x + jy \), we can separate (14) into real and imaginary parts, and assuming a lossy material (so that \( \epsilon \) and therefore \( \ell \) will be complex) then

\[
\pm \ell = \pm (\ell_r + j\ell_i) = \frac{-j(x + jy)}{\cos x \sinh y - j \sin x \cosh y}
\]

and so

\[
\pm [\ell_r \cos x \sinh y + \ell_i \sin x \cosh y] - y = 0 \quad (15)
\]

\[
\mp [\ell_r \cos x \sinh y - \ell_i \sin x \cosh y] - x = 0. \quad (16)
\]

Simultaneous solution of (15) and (16) will yield \( x \) and \( y \) from which \( p \), and then \( \eta \) can be determined.

A similar approach as used in Section III has been adopted in the PEC case. However, unlike the PMC case in Section III it is not possible in the PEC case to ignore the two solutions given by the different signs in (15) and (16). Each of these contribute poles to the final solution, and hence their separate consideration is necessary. Accordingly, in Case I we seek the solution of

\[
[\ell_r \cos x \sinh y - \ell_r \sin x \cosh y] - x = 0 \quad (17)
\]

and

\[
[\ell_r \cos x \sinh y + \ell_i \sin x \cosh y] + y = 0 \quad (18)
\]

whereas in Case II we seek the solution of

\[
[\ell_r \cos x \sinh y - \ell_r \sin x \cosh y] + x = 0 \quad (19)
\]

and

\[
[\ell_r \cos x \sinh y + \ell_i \sin x \cosh y] - y = 0. \quad (20)
\]

Plots of (17), (18) (Case I) and (19), (20) (Case II) are similar in form to that obtained for the PMC case.

A. PEC Case—Surface-Wave Poles

As in the PMC case, the approximate location of the surface-wave poles can be found by setting \( \eta = 0 \). However, we need to consider Case I and Case II separately which yield, from (17) and (19), respectively, the two equations

\[
\text{Case I: } x = -\ell_r \sin x \quad (21)
\]

\[
\text{Case II: } x = \ell_r \sin x. \quad (22)
\]

The solution \( x = y = 0 \) (ie \( \kappa_2 = 0 \)) for both Cases I and II need not be considered further, as it can be shown using L’Hôpital’s rule that the magnitude of (2) remains finite in this case. The remaining part of the procedure (including checking the Riemann sheets) is virtually identical to that for the PMC surface-wave poles.

B. PEC Case—Leaky-Wave Poles

A similar approach can be taken as for the PMC leaky-wave poles, except that Cases I and II need to be considered separately. In Case I, complex solutions for (17) and (18) are seen to occur for \( x \simeq \pm 3\pi/2, \pm 7\pi/2, \pm 11\pi/2, \ldots \), which can be substituted into (17) to give

\[
y = \cosh^{-1} \left( \frac{x}{\ell_r} \right). \quad (23)
\]

Similarly, in Case II, complex solutions for (19) and (20) are seen to occur for \( x \simeq \pm 5\pi/2, \pm 9\pi/2, \pm 13\pi/2, \ldots \), which can be substituted into (19) to give the same result as (23). As with the PMC poles improved poles estimates can be obtained if multidimensional optimization is adopted using the approximate values as seeds.

V. POLE APPROXIMATIONS AND THE SPECTRAL-GAP

The approach presented in Sections III and IV has been shown to yield estimates of both the surface- and leaky-wave pole locations. Of interest is the behavior of the leaky-wave pole “loops,” arising due to (10) in Fig. 1 for the PMC case, and (17) and (19) for the PEC case. These “loops” (the stationary points of which approximate the leaky-wave pole solutions) are seen to vertically converge and join to give solutions that correspond to the surface-wave pole solutions, as the excitation frequency increases. This transitional behavior is consistent with the observations reported in [10]–[12] concerning the spectral-gap region in which a physically meaningful leaky mode transitions to a bound surface-wave mode. In the case of lossless substrates, the spectral-gap behavior is characterized by a split point at which the leaky-wave poles merge to form a double pole, and then separate to ultimately become a proper/improper surface-wave pole pair. Such a split point does not occur for lossy substrates, but it is useful to introduce the qualitative notion of a “split zone” as the nominal region where the leaky-wave poles pass closest to each other.

VI. IMPROVEMENTS

The approximation technique described in Sections III and IV has been shown to yield the greatest accuracy for poles well removed from the split zone. In general, multidimensional numerical optimization can subsequently be used to refine these initial approximations (if required). Conversely, the least accurate initial approximations were obtained when the poles of interest were either within or in close proximity to the split zone—for example, poles “A” and “B” in Fig. 2 and Table I. The initial approximations in this case were still sufficiently accurate to function as valid seeds for the numerical optimizer. However, when considering poles located deep within the split zone, the initial approximations might well prove unreliable for use as seeds. The approximation technique proposed is fundamentally dependent on the specific nature of (11) (PMC) and (18), (20) (PEC) which (in the case of low-loss substrates) exhibit gradients which are either very large or virtually zero. It is this characteristic that makes the approximation of the intersections [and thereby the solutions to the simultaneous equation pairs (10)/(11) (PMC) and (15)/(16) (PEC)] almost trivial. It has also
been observed that large substrate conductivities can cause sufficient distortion in the results plotted in Fig. 1 so as to invalidate these assumptions.

Fortunately, a simple approach can be used to circumvent these difficulties. The key idea behind this approach is to derive approximate solutions (using the method described in Sections III and IV) in a region where the poles of interest are both well removed from the split zone and for substrate conductivities that are not excessive. These approximations can then be tracked toward the solution of interest using estimates calculated at each iteration to seed the next iteration step. Practically, this means commencing the procedure at a sufficiently low frequency such that all poles are leaky, and then gradually increase the frequency tracking the poles until the desired value is obtained. In the case of high-conductivity substrates the equivalent conductivity optimized estimates by the “Δ” symbols. These can then be used to decide whether the approximations derived using the technique in Sections III and IV can be either used directly or after optimization, or whether the iterative approach described in Section VI is necessary.

Alternatively, if \( L_r \) is known, these expressions can be solved for \( n_m \) and \( n_e \) (assumed real) and thus used to determine how many leaky-wave poles have transitioned through the split zone and become surface-wave poles. It should be noted that these expressions only consider the tangent behavior and give no valid solution for \( L_r < 1 \). However, in the PMC case there is at least one surface-wave pole due to the intersection of the linear and \( \cos(\cdot) \) term in (12). The first “split” occurs when the linear and \( \cos(\cdot) \) term in (12) are tangential (corresponding to \( n_m = 1 \)). As each leaky-wave “loop” in Fig. 1 gives rise to two surface-wave poles, the number of surface-wave poles arising from the PMC solution can be written as

\[
N_m = \begin{cases} 
1 & L_r < 1 \\
\left\lfloor \frac{1}{2 |n_m|} \right\rfloor + 1 & L_r \geq 1
\end{cases}
\]
where $\lceil m \rceil$ is the largest integer smaller than or equal to $m$. Similarly, in the PEC case there are no surface-wave poles for $l_r < 1$, and for $l_r \geq 1$ there is only one pole until the linear and $-\sin(\cdot)$ terms are tangential in (21) (corresponding to $n_k \equiv 1$). Accordingly, the number of surface-wave poles arising from the PEC solution is given by

$$N_e = \begin{cases} 0 & l_r < 1 \\ 2\lfloor n_k \rfloor + 1 & l_r \geq 1 \end{cases}$$

in which the number of poles determined for Cases I and II have been combined.

VIII. Conclusion

An approximate technique for locating both the surface-wave and leaky-wave poles for a lossy dielectric slab has been presented. Both PMC and PEC cases have been considered, with both yielding pole solutions that arise from the simultaneous solution of two transcendental equations. Although transcendental in form, in both cases a simple approximate solution for the poles has been derived. The result obtained is very useful since it is yields approximate solutions which are not dependent on the physical geometry, material properties or frequency. In the example considered, the greatest prediction accuracy was observed for surface-wave poles and for leaky-wave poles well removed from the split zone. Multidimensional numerical optimization can be used to refine the pole estimates.

For poles located deep within the split zone or for substrates with large conductivity, the approximation accuracy decreases and the estimates thus obtained may be unsuitable for use as seeds in optimization. For these cases an alternative approach has been proposed which uses estimates from the approximation technique applied in a “stable” zone (removed from split zone), which are then iterated toward the desired solution. An example of a substrate with a large conductivity has been considered to illustrate this procedure.

The behavior of the approximate solutions in the vicinity of the split zone was also investigated and used to derive expressions for the number of proper plus improper surface-wave poles in a given problem.

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