Dependence of gravitational wave transient rates on cosmic star formation and metallicity evolution history

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ABSTRACT
We compare the impacts of uncertainties in both binary population synthesis models and the cosmic star formation history on the predicted rates of gravitational wave (GW) compact binary merger events. These uncertainties cause the predicted rates of GW events to vary by up to an order of magnitude. Varying the volume-averaged star formation rate density history of the Universe causes the weakest change to our predictions, while varying the metallicity evolution has the strongest effect. Double neutron star merger rates are more sensitive to assumed neutron star kick velocity than the cosmic star formation history. Varying certain parameters affects merger rates in different ways depending on the mass of the merging compact objects; thus some of the degeneracy may be broken by looking at all the event rates rather than restricting ourselves to one class of mergers.

Key words: gravitational waves – methods: numerical – galaxies: star formation.

1 INTRODUCTION
Since the detection of the first confirmed gravitational wave (GW) compact binary merger events, astronomers and astrophysicists have been considering how to use this new window on the Universe to place constraints on its contents and our understanding of the underlying physics (e.g. Abbott et al. 2016a, 2017b,c, 2019b). One of the most straightforward observables from GW events is their volumetric rate in the local Universe. A key test of stellar population synthesis codes is to reproduce that observed rate (e.g. Kruckow et al. 2018; Perna et al. 2018; Eldridge, Stanway & Tang 2019). To do this population synthesis codes predict a delay-time distribution: the expected event rate of GW transients versus time for a given amount of star formation. This is then combined with an assumed star formation history, along with its metallicity evolution, to predict a rate at the current epoch (see e.g. Langer & Norman 2006; de Mink & Belczynski 2015; Eldridge et al. 2019). There has been significant study of the how the uncertainties and assumptions in the stellar population models, especially the natal-supernova (SN) kick, affect the rate predictions and the observed double neutron star population (e.g. Fryer, Burrows & Benz 1998; Wex, Kalogera & Kramer 2000; Dominik et al. 2013; Lipunov & Pruzhinskaya 2014; Abbott et al. 2016a; Beniamini & Piran 2016; Beniamini, Hotokezaka & Piran 2016; Belczynski et al. 2017; Tauris et al. 2017; Chruslinska et al. 2018; Kruckow et al. 2018; Mapelli & Giacobbo 2018; Vigna-Gómez et al. 2018; Andrews & Mandel 2019; Eldridge, Stanway & Tang 2019; Giacobbo & Mapelli 2019).

However there are also substantial uncertainties in the star formation history of the Universe and its metallicity evolution that have been largely neglected until recently (Lamberts et al. 2018; Artale et al. 2019; Chruslinska, Nelemans & Belczynski 2019; Mapelli et al. 2019; Neijssel et al. 2019).

In this Letter, we build upon our initial work in Eldridge & Stanway (2016) and Eldridge et al. (2019) to investigate how varying the early star formation history and metallicity evolution of Universe affects the predicted event rate of GW transients. We compare this to the changes in the event rates from changing some of the parameters within our stellar population synthesis models.

2 METHODS, OBSERVATIONS, AND SIMULATIONS
To calculate the GW transient event rate and its redshift evolution, we use the method outlined in Eldridge et al. (2019). Delay-time distributions calculated from the Binary Population and Spectral Synthesis (BPASS)1 v2.2.1 code (Eldridge et al. 2017; Stanway & Eldridge 2018) were combined with a volume-averaged cosmic star formation history (Madau & Dickinson 2014) and a model for the evolution of metallicity in star-forming regions (Langer & Norman 2006). We now build upon this method to investigate how varying the star formation history and/or the cosmic metallicity evolution changes the expected rate of compact binary mergers. Specifically we consider neutron star–neutron star (NS–NS), black hole–neutron star (BH–NS), and black hole–black hole (BH–BH) mergers.

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from multiple sources by Madau & Dickinson 2014) are derived from rest-frame ultraviolet measurements and so are subject to dust correction factors approaching 1 dex. Galaxies at the highest redshifts are currently believed to have very little dust, based on fitting to their spectral energy distributions (Bouwens et al. 2012) but the uncertainties on this are large (Wilkins et al. 2016, 2018). If the intrinsic spectra of these sources are bluer (i.e. younger, lower metallicity or with a higher stellar rotation, and/or multiple fraction) than currently estimated, the dust extinction will be underestimated, pushing the function towards lower u. We evaluate a large range of models to allow for this possibility.

In addition, we calculate the fraction of star formation at different metallicities using the expression of Langer & Norman (2006):

$$\psi \left( \frac{Z}{Z_\odot} \right) = \frac{\Gamma \alpha + 2}{\Gamma (\alpha + 2)} \frac{10^{0.15 z (\alpha + 2)}}{Z_\odot} \frac{Z}{Z_\odot} \frac{\alpha + 2}{\Gamma \alpha + 2} \frac{10^{0.15 z (\alpha + 2)}}{Z_\odot} \frac{(1 + z)^{2.7}}{1 + (1 + z)/2.9^2} \frac{M_\odot}{yr^{-1} Mpc^{-3}}. \quad (2)$$

In this expression the value of \( \beta \) determines how quickly the Universe becomes enriched with metals, \( z \), as a function of redshift \( z \) and how broad the metallicity distribution is at each redshift. While in Eldridge et al. (2019), we used \( \beta = 2 \) here we allow this exponent to vary from 1 to 6. A higher \( \beta \) means the Universe was more quickly enriched, with a smaller metallicity scatter. In Fig. 1, we compare the model metallicity enrichment for different \( \beta s \) to that determined from observations of damped Lyman \( \alpha \) systems (DLAs). We offset the models by \(-0.5 \) dex to correct for the higher impact parameters (and thus lower measured metallicities) of DLAs relative to typical star-forming regions.

Over this cosmic history parameter space we calculate three model grids with different BPASS stellar population synthesis model sets. These are as follows.

(i) BPASSv2.1 (Eldridge et al. 2017) models assume every star is in a binary with a flat distribution in mass ratio and the log of initial period. When a SN occurs, a kick velocity is picked at random from the neutron star kick velocity distribution of Hobbs et al. (2005).

(ii) BPASSv2.2, Hobbs (Stanway & Eldridge 2018) models use the empirical binary population and parameter distributions of Moe & Di Stefano (2017) and are typically more robust for the old stellar populations dominated by low-mass stars. The SN kick is also picked at random from the distribution of Hobbs et al. (2005).

(iii) BPASSv2.2, Bray models use the same v2.2 initial binary parameter distributions as for (ii) but now we use the neutron star kick velocity from the work of Bray & Eldridge (2018):

$$v_{kick2D} / km s^{-1} = 100^{0.30 + 0.20 \left(M_{\odot}/M_{\odot}\right)} - 170^{0.20 - 0.10}.$$

We show the predicted \( z = 0 \) GW event rates for these three BPASS model sets assuming the fiducial cosmic history parameters of \( \beta = 2 \) and \( u = 5.6 \) in Table 1. Varying the initial binary population, mass ratio, and separation distributions has little effect on the NS–NS or NS–BH merger rate, but more than doubles the BH–BH merger rate. This is similar to results found by Mandel & de Mink (2016) and Belczynski et al. (2017). However changing the SN
Table 1. Event rates in Gpc$^{-3}$ yr$^{-1}$ for varying stellar population synthesis assumptions and fiducial cosmic history model ($u = 5.6$, $\beta = 2$). Observational estimates based on the Laser Interferometer Gravitational-Wave Observatory (LIGO) second observing run (O2) are given in the final column from Abbott et al. (2017a) for the NS–NS events, and from Abbott et al. (2019a), their model B, for the BH–BH events. The uncertainties are the 90 per cent confidence limits.

<table>
<thead>
<tr>
<th>Events</th>
<th>v2.1, Hobbs</th>
<th>v2.2, Hobbs</th>
<th>v2.2, Bray</th>
<th>LIGO O2</th>
</tr>
</thead>
<tbody>
<tr>
<td>NS–NS</td>
<td>472</td>
<td>417</td>
<td>2220</td>
<td>$150^{+3200}_{-1200}$</td>
</tr>
<tr>
<td>NS–BH</td>
<td>214</td>
<td>204</td>
<td>352</td>
<td></td>
</tr>
<tr>
<td>BH–BH</td>
<td>51.5</td>
<td>134</td>
<td>59.7</td>
<td>$53.2^{+58.5}_{-28.8}$</td>
</tr>
</tbody>
</table>

We present the results of varying the early star formation rate parameter $u$ and the metallicity evolution parameter $\beta$ in Fig. 2 and provide quantitative values in Table A1 in Appendix A. The trends we observe are relatively simple.

Changing the early amount of star formation by varying $u$ has the weakest impact of our two parameters. Decreasing $u$ leads to greater early star formation and thus increases the number of low metallicity, massive early stars that can produce GW events after a long delay time. As a result the current-epoch rate of BH–BH and BH–NS events at fixed $\beta$ shows a weak tendency to increase at low values of $u$.

In comparison the metallicity evolution parameter $\beta$ has a much stronger effect, changing the merger rate by an order of magnitude for BS–NS and BH–BH mergers. The merger rates are highest at $\beta = 1$, indicating that GW transients prefer a low-metallicity environment. In all cases a higher $\beta$ leads to more metal-rich stars that are typically less efficient at creating BH–BH and BH–NS GW events (e.g. Belczynski et al. 2010; Eldridge & Stanway 2016). This is because higher metallicity stars have stronger stellar winds so lose more mass creating less massive black holes and wider binaries that have longer merger times via gravitational waves.

NS–NS mergers in comparison show much weaker dependence on $\beta$. At the highest $\beta$ values the merger rates reverse their decline and begin to increase instead, especially in models (i) and (iii). This is because as the stellar mass-loss rates increase in high-metallicity stars they become more likely to produce more neutron star than black holes at core collapse. The NS–NS merger rate increases at the expense of mergers involving black holes. We note that the almost flat dependence of the NS–NS merger rate on the star formation parameters shows that this rate is more dependent on the stellar evolution model parameters than the star formation history.

This confirms that the relative rates of different classes of events from LIGO/Virgo Consortium observations will have diagnostic power in distinguishing between physically motivated models for both stellar physics effects and cosmic evolution histories.

On each of the panels (Fig. 2), we include lines representing the current observational constraints on rates (Abbott et al. 2016b, 2019a). For the BH–BH mergers, models with $\beta$ close to 2 give values in good agreement with observations, suggesting that our fiducial model is a reasonable match to the observed Universe, although a range of $\beta$ from 1 to 3 is also consistent with the rate uncertainties.

The current observationally inferred NS–NS merger rate is significantly higher than most extant population synthesis codes predict (Chruslinska et al. 2018, 2019; Mapelli & Giacobbo 2018). However, novel kick schemes or a different metallicity evolution history of the Universe have been shown to push predictions close to the observed constraint, with the highest being that from using the kick of Bray & Eldridge (2018) as we see here. Both models (i) and (ii) are at the lower bound of observed rate, while model (iii) is at the upper bound. This indicates that the assumed kick distribution may lie between these estimates and that GW event rates may prove an effective constraint on this distribution. Finally all cases with $\beta = 2$ yield predictions in good agreement with current upper limits on the NS–BH merger rate.

4 DISCUSSION AND CONCLUSIONS

It is clear from our results that adopting different assumptions for the star formation and metallicity evolution of the Universe can have a significant effect on current epoch compact binary merger rates. These are as important, if not more so for the metallicity evolution, than changing the input physics of the binary interactions. We have found that the highest merger rates are obtained for low values of $\beta$ with little dependence on the values of $u$. However this primarily affects the merger rates involving black holes, the NS–NS merger rate depends only very weakly on the star formation history.

Thus by using the different merger rates it may be possible to break the degeneracy between binary evolution and cosmic history uncertainties. We note that our results are in line with other recent work in highlighting the importance of the metallicity evolution in predicting the correct merger rates (Chruslinska et al. 2019; Neijssel et al. 2019).

For model (i) (BPASS 2.1, Hobbs), varying $u$ and $\beta$ changes the predicted NS–NS rate from the fiducial value by $<10$ per cent in all cases except that of the lowest $\beta$ that reaches 18 per cent at $u = 4$. By contrast the NS–BH rate can vary by as much as 67 per cent from the fiducial value, and the BH–BH rate can vary by 90 per cent of the fiducial value.

For model (ii) (BPASS 2.2, Hobbs), varying $u$ and $\beta$ changes the predicted NS–NS rate from the fiducial value by $<7$ per cent, the NS–BH rate by up to 77 per cent, and the BH–BH rate by up to 80 per cent of the fiducial value.

For model (iii) (BPASS 2.2, Bray), the pattern is similar with the predicted NS–NS rate varying from the fiducial value by $<10$ per cent across all parameters other than $\beta = 1$ that can reach a 43 per cent variation at low $u$. The NS–BH and BH–BH rates both
Figure 2. BPASS predictions for the merger rates of NS–NS, BH–NS, and BH–BH mergers with different models. The solid lines are for model (i) v2.1, the dotted lines are for model (ii) v2.2, and the dashed lines for model (iii) v2.2 with the Bray kick. The solid horizontal grey lines indicate the best estimate for the merger rates from Abbott et al. (2016b, 2019a), while the dashed lines are the lower limits and the dash–dotted lines are the upper limits. For NS–NS, BH–NS, and BH–BH mergers rates these are taken to be $1540 \pm 3200$, $<610$, and $53.2 \pm 58.5$ Gpc$^{-3}$ yr$^{-1}$, respectively.

vary by a factor of 2 relative to the fiducial value over the parameter range explored.

In all cases, the variation seen (within a factor of 2) suggests that the current observation of the NS–BH and BH–BH rates would struggle to discriminate between cosmic histories, given their substantial uncertainties. Measurements with a precision of a few per cent will be required to do so, which may also lie beyond the capability of the current observing run (LIGO/Virgo Consortium third observing run, LVC O3).

By contrast, we have demonstrated that discriminating between the underlying assumptions of the stellar population synthesis models may be possible with weaker observational data. Changing the initial binary distribution (from v2.1 to v2.2) modestly reduces NS–NS and NS–BH events by ~5–10 per cent but causes a dramatic, factor of 2.6, increase in the BH–BH rates due to the larger number of close binaries occurring in a stellar population of a given total initial mass using the updated prescription. More pronounced still is the effect of changing the SN kick prescription, which boosts the rate of NS–NS mergers by almost an order of magnitude, since more low-mass systems survive their two-SN evolution pathways without being disassociated. Importantly, we notice that the impact of changing cosmic history input parameters and physical model of stellar population synthesis vary by compact binary type. While interpreting event rates of one type (e.g. NS–NS) will lead to degenerate explanations, this degeneracy can be broken by comparing the rates of different types simultaneously. This implies that attempting to match the observed merger rate of these events at the same time will allow us to constrain our understanding of various aspects of stellar physics and also the evolution of the Universe. A consistent picture from our results is that changing the assumed star formation history or metallicity evolution away from their current fiducial parameters generally leads to a decreased GW event rate. The predicted GW event rate only increases with an (unlikely) increase in the amount of stars formed in the early Universe. This would likely put the cosmic star formation rate density history in tension both with direct observations of the early universe (e.g. Bouwens et al. 2019) and with the observed history of mass assembly (which should follow its integral; see Madau & Dickinson 2014; Wilkins, Lovell & Stanway 2019). Alternatively a higher rate may be possible with a much slower metallicity evolution that is at odds with the observed early enrichment of the Universe (with relatively high metallicities being measured out to $z > 3$, see e.g. Sanders et al. 2020, and Fig. 1). The forthcoming James Webb Space Telescope will place much improved direct constraints on the properties of early star formation. In particular, it will improve observations of galaxies in the rest-frame optical (with its relative insensitivity to dust extinction) and permit the true star formation rate density and metallicity at high redshift to be determined at unprecedented precision. While this work is already making progress from the ground at $z \sim 2–3$ (e.g. Steidel et al. 2016; Sanders et al. 2019), the sensitivity, wavelength coverage, and multiplexing capability of the Near-Infrared Spectrograph (NIRSpec) will permit determination of precise metallicities directly in the star-forming galaxies that are responsible for the large delay-time tail of the GW event distributions.

We note that predictions from BPASS stellar population synthesis models, when combined with the adopted fiducial star formation history and metallicity evolution of $u = 5.6$ and $\beta = 2$ (from Madau & Dickinson 2014 and Langer & Norman 2006, respectively), are in good agreement with the current LIGO/Virgo BH–BH and NS–NS merger rate estimates. The high NS–NS rate derived from GW 170817 favours model (iii), BPASS v2.2 with a Bray & Eldridge (2018) SN kick, in particular. If the NS–NS merger rate derived in the current and future LIGO/VIRGO observing runs is indeed as high as we predict, this will provide further support for adoption of a revised neutron star kick distribution in future work. Combining predicted event rates with the chirp mass distribution will provide further constraints on stellar and cosmic evolution models, although care will be needed to account for the impact of chirp mass on detectability of systems when comparing models to data.

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APPENDIX A: TABULATED RESULTS OF GW EVENT RATES

<table>
<thead>
<tr>
<th>Model</th>
<th>Method</th>
<th>Rate [Gpc$^{-3}$ yr$^{-1}$]</th>
</tr>
</thead>
<tbody>
<tr>
<td>i</td>
<td>(i)</td>
<td>1.97 ± 0.12</td>
</tr>
<tr>
<td>ii</td>
<td>(ii)</td>
<td>2.01 ± 0.08</td>
</tr>
<tr>
<td>iii</td>
<td>(iii)</td>
<td>2.04 ± 0.10</td>
</tr>
</tbody>
</table>

Note: The rates are given for three different models: (i), (ii), and (iii). The uncertainties are quoted at the 1σ level.